

# DPP No. 31

**Total Marks: 22** 

Max. Time: 22 min.

Topics: Newtons's Law of Motion, Projectile Motion, Friction

Type of Questions

Single choice Objective ('-1' negative marking) Q.1 to Q.6 Multiple choice objective ('-1' negative marking) Q.7

(3 marks, 3 min.) (4 marks, 4 min.) M.M., Min. [18, 18] [4, 4]

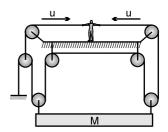
1. System is shown in the figure and man is pulling the rope from both sides with constant speed 'u'. Then the speed of the block will be:

(A)  $\frac{3u}{4}$ 

(B)  $\frac{3u}{2}$ 

(C)  $\frac{u}{4}$ 

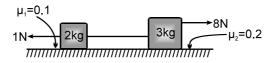
(D) none of thes



2. Hailstones falling vertically with a speed of 10 m/s, hit the wind screen (wind screen makes an angle 30° with the horizontal) of a moving car and rebound elastically. The velocity of the car if the driver finds the hailstones rebound vertically after striking is:

- (A)  $10\sqrt{3}$  m/s
- (B)  $20\sqrt{3}$  m/s
- (C) 10 m/sec
- (D)  $\frac{10}{\sqrt{3}}$  m/sec

3. In the shown arrangement if  $f_1$ ,  $f_2$  and T be the frictional forces on 2 kg block, 3kg block & tension in the string respectively, then their values are:



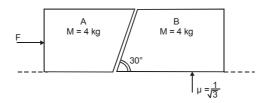
(A) 2 N, 6 N, 3.2 N

(B) 2 N, 6 N, 0 N

(C) 1 N, 6 N, 2 N

(D) data insufficient to calculate the required values.

Two blocks A and B are placed in contact on a horizontal surface. Faces of blocks A and B, which are in contact, are inclined at 30° with the horizontal, as shown. There is no friction between block A and any surface which is in contact with this whereas friction coefficient between block B and the surface is  $\frac{1}{\sqrt{3}}$ . A force F is applied in horizontal direction on block A. What is the minimum value of F at which the block B just start moving rightwards?



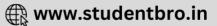
(A)  $\frac{40}{\sqrt{3}}$ N

(B)  $\frac{80}{\sqrt{3}}$ N

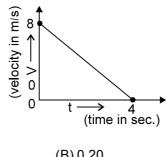
(C) 100 N

(D) For any value of F, motion will not start



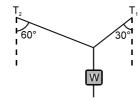


5. A block of mass 2 kg is given a push for a moment horizontally and then the block starts sliding over a horizontal plane. The graph shows the velocity-time graph of the motion. The co-efficient of sliding friction between the plane and the block is:

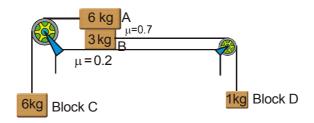


- (A) 0.02
- (C) 0.04

- (B) 0.20
- (D) 0.40
- 6. A weight W is supported by two strings inclined at 60° and 30° to the vertical. The tensions in the strings are T<sub>1</sub> & T<sub>2</sub> as shown. If these tensions are to be determined in terms of W using a triangle of forces, which of these triangles should you draw? (block is in equilibrium)



- 7. An arrangement of the masses and pulleys is shown in the figure. Strings connecting masses A and B with pulleys are horizontal and all pulleys and strings are light. Friction coefficient between the surface and the block B is 0.2 and between blocks A and B is 0.7. The system is released from rest. (use  $g = 10 \text{ m/s}^2$ )



- (A) The magnitude of acceleration of the system is 2 m/s<sup>2</sup> and there is no slipping between block A and
- (B) The magnitude of friction force between block A and block B is 42 N.
- (C) Acceleration of block C is 1 m/s<sup>2</sup> downwards.
- (D) Tension in the string connecting block B and block D is 12 N.



### **DPP NO. - 31**

- **1.** (A)
- **2**. (A)
- **3.** (C)
- **4.** (D)
- **5.** (B)

- **6.** (E)
- **7.** (A)(D)

## **Hint & Solutions**

### **DPP NO. - 31**

1. 
$$u = \frac{0 + v_1}{2}$$
,  $\frac{v_1 + v_2}{2} = v$ ,  $\frac{-v_2 + u}{2} = v$ 

Hence v = velocity of M =  $\frac{3u}{4}$ .

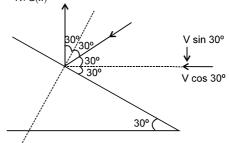
For the driver to observe the rain move vertically upward after the elastic collision, rain should come at an angle 30° with the horizontal (as clear from figure).

Let , velocity of rain w.r.t. car be  $V_{m/c}$ 

$$\vec{V}_{R/G} = \vec{V}_{R/C} + \vec{V}_{C/G}$$

$$\vec{V}_{R/G(x)} = \vec{V}_{R/C(x)} + \vec{V}_{C/G(x)}$$

But  $\vec{V}_{R/G(x)} = 0$ , since rain fall vertically down.



$$\Rightarrow \vec{V}_{C/G(x)} = -\vec{V}_{R/C(x)} = -(V \cos 30^{\circ})$$

$$\Rightarrow |\vec{V}_{C/G(x)}| = V \cos 30^{\circ} \dots (i)$$

Now, 
$$\vec{V}_{R/G(y)} = \vec{V}_{R/C(y)}$$

$$\Rightarrow$$
 -10 = -V sin 30° + 0

[Since ; 
$$V_{R/G(y)} = -10 \text{ m/s}$$
 ;  $V_{C/G(y)} = 0$ ]

$$\Rightarrow$$
 V sin 30° = 10  $\Rightarrow$  V = 20 m/s.

Substituting V = 20 m/s in equation (i)

$$\vec{V}_{C/G(x)} = V \cos 30^{\circ} = 20 \times \frac{\sqrt{3}}{2} = 10 \sqrt{3} \text{ m/s}.$$

$$\vec{\nabla}_{C/G} = 10\sqrt{3} \hat{j} \text{ m/s}.$$





Net force without friction on system is '7N' in right side so first maximum friction will come on 3 kg block.

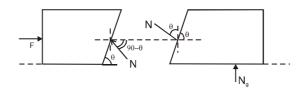
So 
$$f_1 = 1 N$$
,  $f_2 = 6 N$ ,  $T = 2N$   
 $f_1 = 1 N$ ,  $f_2 = 6 N$ ,  $T = 2N$ 

4. 
$$F = N \sin \theta$$
  $N = \frac{F}{\sin \theta}$ 

$$N \sin \theta = \mu (N \cos \theta + mg)$$
$$F = \mu(F \cot \theta + mg)$$

$$F(1 - \mu \cot \theta) = \mu mg$$

$$F = \frac{\mu mg}{1 - \mu \cot \theta}$$



On putting 
$$\mu = \frac{1}{\sqrt{3}}$$
 and  $\theta = 30^{\circ}$ 

$$\mu = \frac{1}{\sqrt{3}} \quad \theta = 30^{\circ}$$

Therefore motion will not start for any value of F.

#### 5. The magnitude of deceleration from graph is

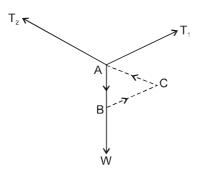
$$a = \frac{8-0}{4-0} = 2m/s^2$$

The deceleration of block is

$$a = \mu g$$
  $\therefore \mu = \frac{a}{g} = 0.2$ 



**6.** 
$$\overrightarrow{AB} = \overrightarrow{W}$$
,  $\overrightarrow{BC} = \overrightarrow{T_1}$ ,  $\overrightarrow{CA} = \overrightarrow{T_2}$   
 $\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CA} = 0$ 



Ans. (E)

7. Suppose blocks A and B move together. Applying

$$60 - T = 6a$$

$$T - 18 - T' = 9a$$

$$T' - 10 = 1a$$

Solving  $a = 2 \text{ m/s}^2$ 

To check slipping between A and B, we have to find friction force in this case. If it is less than limiting static friction, then there will be no slipping between A and B.

Applying NLM on A.

$$T - f = 6(2)$$

$$f = 36 N$$

and  $f_s = 42 \text{ N}$  hence A and B move together.

and तथा T' = 12 N.

